APPLICATION FOR UNITED STATES LETTERS PATENT

INVENTOR:

Raghavan SUDHAKAR

Austin, Texas

TITLE:

COMPUTATION OF LOGARITHMIC AND

EXPONENTIAL FUNCTIONS

ASSIGNEE:

Intel Corporation

Santa Clara, California

ATTORNEYS/

AGENTS:

Venable, LLP

Box 34385

Washington, DC 20043-9998 Telephone: (202) 344-4000 Facsimile: (202) 344-8300

ATTORNEY

DOCKET NO.:

42339-199423

BACKGROUND OF THE INVENTION

[0001] In addition to their roles in mathematical libraries, logarithmic and exponential functions (or anti-logarithms) of real numbers play important roles in many applications. For example, in wireless communications, such functions may arise in computing received signal strength indicators (RSSIs), log-likelihood ratios in demodulators and decoders, etc. Further contexts in which they also may arise include speech compression and coding, image contrast enhancement, cryptography and reliability analyses, and digital signal processor (DSP) design. However, many past implementations of these functions have lacked desired speed and/or accuracy.

BRIEF DESCRIPTION OF THE DRAWINGS

[0002] Various embodiments of the invention will now be described in connection with the associated drawings, in which:

[0003] Figures 1A and 1B depict flowcharts of computational methods for logarithmic functions according to exemplary embodiments of the invention;

[0004] Figure 2 depicts a flowchart of a computational method for exponential functions according to an exemplary embodiment of the invention;

[0005] Figures 3A, 3B, 3C, 3D, and 3E depict conceptual block diagrams of systems implementing exemplary embodiments of the invention;

[0006] Figures 4A and 4B depict flowcharts of computational methods for logarithmic and exponential functions using the system of Figure 3, according to exemplary embodiments of the invention;

[0007] Figure 5 depicts a system according to an embodiment of the invention; and

[0008] Figure 6 depicts a conceptual block diagram of a computer system that may be used to implement an embodiment of the invention.

[0009] In the following description, numerous specific details are set forth. However, it is understood that embodiments of the invention may be practiced without these specific details. In other instances, well-known circuits, structures, and/or techniques have not been shown in detail in order not to obscure an understanding of this description.

[0010] References to "one embodiment", "an embodiment", "example embodiment", "various embodiments", etc., indicate that the embodiment(s) of the invention so described may include a particular feature, structure, or characteristic, but not every embodiment necessarily includes the particular feature, structure, or characteristic.

Further, repeated use of the phrase "in one embodiment" does not necessarily refer to the same embodiment, although it may.

[0011] In the following description and claims, the terms "coupled" and "connected," along with their derivatives, may be used. It should be understood that these terms are not intended as synonyms for each other. Rather, in particular embodiments, "connected" may be used to indicate that two or more elements are in direct physical or electrical contact with each other. "Coupled" may mean that two or more elements are in direct physical or electrical contact. However, "coupled" may also mean that two or more elements are not in direct contact with each other, but yet still co-operate or interact with each other.

[0012] An algorithm is here, and generally, considered to be a self-consistent sequence of acts or operations leading to a desired result. These include physical manipulations of physical quantities. Usually, though not necessarily, these quantities take the form of electrical or magnetic signals capable of being stored, transferred, combined, compared, and otherwise manipulated. It has proven convenient at times, principally for reasons of common usage, to refer to these signals as bits, values, elements, symbols, characters, terms, numbers or the like. It should be understood, however, that all of these and similar terms are to be associated with the appropriate physical quantities and are merely convenient labels applied to these quantities.

[0013] Unless specifically stated otherwise, as apparent from the following discussions, it is appreciated that throughout the specification discussions utilizing terms such as "processing," "computing," "calculating," "determining," or the like, refer to the action and/or processes of a computer or computing system, or similar electronic computing device, that manipulate and/or transform data represented as physical, such as electronic, quantities within the computing system's registers and/or memories into other data similarly represented as physical quantities within the computing system's memories, registers or other such information storage, transmission or display devices.

[0014] In a similar manner, the term "processor" may refer to any device or portion of a device that processes electronic data from registers and/or memory to transform that electronic data into other electronic data that may be stored in registers and/or memory.

A "computing platform" may comprise one or more processors.

[0015] Embodiments of the present invention may include apparatuses for performing the operations herein. An apparatus may be specially constructed for the desired purposes, or

it may comprise a general purpose device selectively activated or reconfigured by a program stored in the device.

[0016] Embodiments of the invention may be implemented in one or a combination of hardware, firmware, and software. Embodiments of the invention may also be implemented as instructions stored on a machine-accessible medium, which may be read and executed by a computing platform to perform the operations described herein. A machine-accessible medium may include any mechanism for storing or transmitting information in a form readable by a machine (e.g., a computer). For example, a machine-accessible medium may include read only memory (ROM); random access memory (RAM); magnetic disk storage media; optical storage media; flash memory devices; electrical, optical, acoustical or other form of propagated signals (e.g., carrier waves, infrared signals, digital signals, etc.), and others.

[0017] It may be noted that, in general, if one is capable of computing base-2 logarithms and exponentials, one may obtain other logarithmic and exponential functions based on these results by means of constant multiplication. For example, $ln(Y) = (0.6391)(log_2Y)$, $log_{10}Y = (0.3010)(log_2Y)$, $e^X = 2^{1.4427X}$, and $10^X = 2^{3.3219X}$. Hence, if one has methods for obtaining base-2 logarithms and exponentials, the same methods may be used to compute other logarithmic and exponential functions.

[0018] Figures 1A and 1B depict flowcharts showing ways of computing the base-2 logarithm of a number Y according to various embodiments of the invention. A way in which the base-2 logarithm of Y may be computed is to compare Y to a power of 2, beginning from a greatest power of 2 under consideration. If Y is greater than or equal to the power of 2 under consideration, a bit corresponding to that power of 2 in a binary

representation of log₂Y may be set to 1; otherwise, that same bit may be set to 0. This method may be implemented according to the flowchart of Figure 1A.

[0019] In Figure 1A, in block 11, Y may be input. Prior to determining log₂Y, a number of bits may be set for a binary representation of log₂Y, of which some may represent an integer portion of log₂Y, and some may represent a decimal portion of log₂Y. Beginning with a most significant bit (MSB) of this binary representation of log₂Y, block 12 may determine whether or not all bits of the binary representation of log₂Y have been considered. If all bits have been considered, the process may be complete. Otherwise, the process may consider a next bit of the representation, to be denoted b_j, and may accordingly proceed to block 13.

[0020] In block 13, the process may determine if Y is greater than or equal to a jth power of 2, denoted K_j. To understand this, it may be useful to consider that a number, Y, may be expressed as $2^{\log_2 Y}$. $\log_2 Y$, in turn, may be expressed in the form $\cdots + b_2 2^2 + b_1 2^1 + b_0 2^0 + b_{-1} 2^{-1} + b_{-2} 2^{-2} + \cdots$, where, as discussed above, b_j represents the jth bit of the binary representation of $\log_2 Y$, $\ldots b_2 b_1 b_0 .b_{-1} b_{-2} \ldots$ Given this, Y may further be expressed in the form $\cdots K_2^{b_2} \cdot K_1^{b_1} \cdot K_0^{b_0} \cdot K_{-1}^{b_{-1}} \cdot K_{-2}^{b_{-2}} \cdots$, where $K_j = 2^{2^j}$. These are the values of K_i that may be tested against Y in block 13.

[0021] If $Y \ge K_j$, then b_j may be set equal to 1, block 15, and K_j may be removed from Y by division, block 16 (i.e., $Y = Y/K_j$). The process may then loop back to block 12 to determine if there are further bits to consider. If, on the other hand, $Y < K_j$, b_j may be set equal to 0, block 14, and the process may, once again, loop back to block 12.

[0022] The flowchart of Figure 1B presents a variation on the flowchart of Figure 1A. In particular, the division by K_j (i.e., in block 16) may be accomplished, equivalently, by a multiplication by $L_j = 1/K_j$. This is reflected in block 16' and is also used to present an alternative test that may be applied in block 13'. To further explain, the test of block 13' may be observed to be identical to that of block 13 (of Figure 1A) by noting that both sides of the inequality of block 13 may be divided by K_j , and L_j may then be substituted for $1/K_j$.

[0023] Figure 2 depicts a flowchart showing an exemplary method of computing a base-2 exponential function, according to an embodiment of the invention. In other words, the flowchart may be used to compute $Y = 2^X$. As above, X may be considered in binary form as $\dots b_2 b_1 b_0 \dots b_{-1} b_{-2} \dots$, and therefore, $2^X = \dots K_2^{b_2} \cdot K_1^{b_1} \cdot K_0^{b_0} \cdot K_{-1}^{b_{-1}} \cdot K_{-2}^{b_{-2}} \dots$. Hence, Y may be computed by a product of all K_j for which $b_j=1$ (note that when $b_j=0$, $K_j^{b_j} = K_j^0 = 1$). This may be implemented by the flowchart of Figure 2.

[0024] In Figure 2, X may be input, and Y may be initially set equal to one, block 21. In block 22, the process may determine if all bits b_j of the binary representation of X have been considered. If there is still a bit b_j to consider, the process may continue to block 23, where it may test if $b_j=1$. If $b_j=1$, then the process may continue to block 24, and Y may be computed as $Y = Y \cdot K_j$. The process may then loop back to block 22 to test if there are further bits to examine. If, on the other hand, $b_j=0$, the process may simply loop back to block 22 from block 23.

[0025] It may be possible to obtain computational savings in computing both the base-2 logarithm of a number and the base-2 exponential of a number by separately considering integer and non-integer portions. In particular, it may be noted that the integer portion of

the base-2 logarithm of a number Y may be determined simply by examining the binary representation of Y and determining the power of 2 corresponding to the MSB of that binary representation. For example, in the case of $Y=(99)_{10}=(1100011)_2$, the MSB of the binary representation of Y occurs in the position corresponding to 2^6 , so the integer portion of $\log_2 Y$ may be set equal to 6.

[0026] In the case of an exponential function, it may be noted that, in a computer, multiplications by powers of 2 may be accomplished by shift operations. Hence, once the non-integer portion of 2^X is computed, it may be left-shifted, accordingly, to account for the integer portion.

[0027] As a result of these observations, in both the computation of base-2 logarithmic functions and the computation of base-2 exponential functions, computational savings may be realized by considering the integer portions separately and only using processes, such as those depicted in the flowcharts of Figures 1A, 1B, and 2, for the non-integer portions.

[0028] The above-described processes may suggest hardware implementations that may be used to efficiently compute base-2 logarithmic and/or exponential functions. In particular, Figure 3A provides a block diagram of an apparatus that may be used to implement either or both functions, according to an embodiment of the invention. In Figure 3A, the apparatus may include a first register 31 and a coefficient register 32. Register 31 may be used to store the number Y, as used above, in computing either the logarithm or the exponential function. Coefficient register 32 may be used to store either L_j or K_j, depending upon the function being implemented. Since, in some embodiments of the invention, the coefficients may be required only for computation of the fractional

portion of the result, only the negatively-indexed coefficients (i.e., L_i or K_i for j less than zero) may need to be stored. The coefficients may, in some embodiments of the invention, be stored in one or more machine-accessible media, such as look-up tables (LUTs), read-only memories (ROMs), random access memories (RAMs), disks, etc., and read from the machine accessible medium or media into coefficient register 32. The contents of register 31 and coefficient register 32 may be provided to multiplier 33. In an exemplary embodiment of the invention, multiplier 33 may be a 16x16 fractional unsigned multiplier, and each of registers 31 and 32 may be a 16-bit register (as well as registers 34 and 35, which will be discussed below). The output of multiplier 33, which may represent the product of the contents of registers 31 and 32, may be stored in a product register 34. Note that in the exemplary embodiment of the invention in which a 16x16 fractional unsigned multiplier and 16-bit registers may be used, as discussed above, the two 16-bit unsigned inputs from registers 31 and 32 may be multiplied (as unsigned integers) to obtain a 32-bit intermediate result, whose upper sixteen bits may be rounded and placed into the 16-bit product register 34. The contents of product register 34 and register 31 may be fed to a multiplexer 36 whose output may be used as a next input to be loaded into register 31. Which output is fed to register 31 may be determined by a select signal (not shown) that may depend upon which function is being computed. The apparatus of Figure 3A may also include a further register 35, which may be used to store a number X, as used in the discussions above (i.e., in the case of the logarithm, X= log_2Y , and in the case of the exponential, $Y=2^X$); in the case of the logarithm, this may be the result, and in the case of the exponential, this may be an initial number whose

exponential may be computed. The specific uses of register 35 will be further discussed below.

[0029] Figure 3B shows an adaptation of the apparatus of Figure 3A according to an embodiment of the invention. The apparatus of Figure 3B may be used to compute the base-2 logarithm of a number Y. In the embodiment of Figure 3B, the coefficients may correspond to the Li's discussed above. Furthermore, register 31 may be initialized to contain Y; in some embodiments, in which only the non-integer portion is computed by the methods discussed above, register 31 may be initialized with the non-integer portion of Y, left-shifted such that the MSB of Y is left-justified, and in those same embodiments, register 35 may be initialized with the integer portion of log₂Y. In Figure 3B, the MSB of product register 34 may provide each successive bit of the fractional portion of log₂Y for shifting into register 35 (i.e., register 35 may be left-shifted with the MSB of product register 34 as the input bit for each successive bit, as it is determined) and may be used to select whether or not the contents of product register 34 replace Y in register 31 for computing the next bit of log₂Y. Referring back to Figure 1B, this may implement the operations described in blocks 13', 14, 15, and 16' in that the product register 34 may contain $Y \cdot L_i$, whose MSB may represent b_i , which may be one or zero, depending upon whether the product is greater than or equal to one or less than one. [0030] Similarly, Figure 3C shows an adaptation of the apparatus of Figure 3A according to a further embodiment of the invention. The apparatus of Figure 3C may be used to compute the base-2 exponential of a number X. In Figure 3C, the coefficients may correspond to the K_i's discussed above. Register 31, which may ultimately store the desired result, is initialized. If, as discussed above in connection with some embodiments of the invention, only the fractional portion of Y is being computed by the apparatus of Figure 3C, register 31 may be set to all ones; in other embodiments, Y may be set equal to one. Register 35 may be initialized with X. For each successive bit of X, beginning with the least significant bit (LSB), the LSB of X may be used to select whether the contents of the product register 34 or the contents of register 31 may be loaded into register 31 to provide the next value of Y. Hence, register 35 may be right-shifted to provide each successive bit. Referring back to Figure 2, the apparatus of Figure 3C may implement the operations of blocks 23 and 24 in that product register 34 may contain the product $Y \cdot K_j$, and this product may or may not become the next Y, depending upon the value of the LSB of register 35, which may provide b_j .

[0031] Figure 3D shows an adaptation of the apparatus of Figure 3A according to a further embodiment of the invention. The apparatus of Figure 3D may be used to compute the base-2 exponential of a number X and is a variation on the embodiment of Figure 3C. As in Figure 3C, the coefficients may correspond to the K_j's discussed above. Register 31, which may ultimately store the desired result, is initialized. If, as discussed above in connection with some embodiments of the invention, only the fractional portion of Y is being computed, register 31 may be set to all ones; in other embodiments, Y may be set equal to one. Register 35 may be initialized with X. For each successive bit of X, beginning with the least significant bit (LSB), the LSB of X may be used to select whether the contents of the coefficient register 32 or all ones may be input into multiplier 33 to form a product with the contents of register 31, and thus to provide the next value of Y. This is reflected by the use of multiplexer 311, which may use the LSB of X input as a select input (if the LSB of X is zero in Figure 3D, all ones are input; if the LSB of X

is one, the coefficient is input). Note that multiplexer 311 should not be understood as being strictly limited to a multiplexer, but rather, it may comprise any appropriate selection logic, known or as yet to be developed. Hence, register 35 may be right-shifted to provide each successive bit. Referring back to Figure 2, the apparatus of Figure 3D may implement the operations of blocks 23 and 24 in that product register 34 may contain the product $Y \cdot K_j$, and this product may become the next value of Y and may be loaded into register 31.

[0032] It may be noted that a further variation on the embodiment of the invention shown in Figure 3D may switch the order of coefficient register 32 and multiplexer (or other selection logic) 311. That is, multiplexer 311 may receive as inputs both a coefficient and a constant value (which may be all ones in the case of computing the fractional portion of a base-2 exponential function), and the selected input may be provided for loading into coefficient register 32.

[0033] One difference that may be noted in the operations carried out by Figures 3B and 3C/3D is the order in which bits are considered. In Figure 3B, the MSB of the product register may provide the next highest-order bit of the result, and accordingly, the coefficients Lj are considered from j equal to the highest-order bit designation (e.g., in an embodiment of the invention in which only fractional portions of the result are being computed, if the highest order bit were to correspond to 2⁻¹ (j=-1), the process might begin by loading L₋₁ into coefficient register 32) to the lowest-order bit designation (e.g., if the lowest order bit were to correspond to 2⁻⁶ (j=-6), L₋₆ might be the last coefficient to be loaded). In contrast, in Figures 3C and 3D, the LSB of the number whose exponential is to be computed may provide the next bit to be considered; that is, the apparatus may

proceed from lowest order to highest order (bits of the exponent). For example, in the case of j=-1 to -6, the apparatus may load K_{-6} first and K_{-1} last.

[0034] Figure 3E provides a further embodiment of the apparatus of Figure 3A, which may be configured so as to be useful in computing a base-2 logarithm or a base-2 exponential. As discussed above, the coefficients to be used in computing either or both of the logarithm and the exponential may be pre-computed and stored in one or more LUTs (or other machine-accessible media). In Figure 3E, the L_i's that may be used for computing logarithms may be stored in a log LUT 37, and the K_i's that may be used in computing exponentials may be stored in an exp LUT 38. A function selection signal, labeled "LOG/EXP" in Figure 3E, may be used as a select input to multiplexer 39 (which may be embodied, alternatively, as any other selection logic) to determine whether the coefficients are chosen from LUT 37 or LUT 38. It may be noted that, in the specific embodiment shown in Figure 3E, LOG/EXP=1 has been arbitrarily chosen to designate computation of a logarithm, and LOG/EXP=0 has been arbitrarily chosen to designate computation of an exponential. However, one of ordinary skill in the art would understand that these designations may be reversed, enhanced, etc., as desired. The LOG/EXP signal may also be provided as a SHIFT SELECT input to register 35, to determine whether register 35 may shift right or shift left.

[0035] In addition to the above, the computations of logarithm and exponential may utilize either the MSB of product register 34 or the LSB of register 35, respectively, to be provided as a select input to multiplexer 36 to determine the next contents that may be loaded into register 31. To accommodate this, a multiplexer (or other selection logic) 310

may be provided with the aforementioned MSB and LSB and may use the LOG/EXP signal as a select input to determine which may be forwarded to multiplexer 36.

[0036] Finally, while not shown in Figure 3E, additional logic may be provided to account for different initial values that may be loaded into registers 31 and 35. Such additional logic may employ further multiplexers and/or other selection logic to determine, based on, for example, the LOG/EXP signal, appropriate values that may be initially loaded. The initial values may depend upon the desired object of the computation (e.g., logarithm or exponential).

[0037] Figures 4A and 4B depict flowcharts of exemplary processes utilizing the apparatus of Figures 3A-3E, according to some embodiments of the invention. The process depicted in Figure 4A may be used to compute the base-2 logarithm of a number, Y. Accordingly, as reflected in block 41, if, for example, the apparatus shown in Figure 3D were to be used, the LOG/EXP signal may be set to one, to reflect that the desired operation is logarithm. Also in block 41, the number Y may be loaded, for example, into register 31, and a register that may later contain the result of the computation, e.g., register 35, may be initialized. In some embodiments of the invention, as discussed above, only the left-justified fractional portion of Y may be loaded, and the result register may be initialized to contain the integer portion of the result (which may be predetermined, as discussed above).

[0038] As discussed above, the method of computing the logarithm may proceed beginning with the bit position corresponding to the MSB of Y (or, in some embodiments, of the fractional portion of Y). In block 42, the process may determine if there are any further bits (i.e., bit positions) to consider. If not, the process may be

complete. Otherwise, the process may proceed to block 43 and may load a coefficient, L_j , corresponding to a next bit position, into, for example, coefficient register 32. The process may then use, for example, multiplier 33 to compute the product $Y \cdot L_j$, block 44. The process may next proceed to block 45 and left-shift the result register (e.g., register 35) using the MSB of the product, $Y \cdot L_j$, as an input bit. Also, in block 46, the process may determine, based on the value of the MSB of the product, $Y \cdot L_j$, whether the next value of Y (e.g., in register 31) may be loaded to the product, $Y \cdot L_j$, or may remain the same (e.g., reloaded with the same value of Y). The process may then loop back to block 42 and may determine whether there are still bits to consider.

[0039] The process depicted in Figure 4B may be used to compute the base-2 exponential of a number, X. Accordingly, as reflected in block 41', if, for example, the apparatus shown in Figure 3E were to be used, the LOG/EXP signal may be set to zero, to reflect that the desired operation is exponential. Also in block 41', the result, Y, may be initialized, for example, in register 31 (in the case in which the fractional portion is computed, as in some embodiments, Y is initialized to be all ones). Additionally, the number, X, may be loaded into the apparatus (e.g., into register 35); as discussed above, in some embodiments, only the fractional portion of X may be loaded.

[0040] As discussed above, the bits of X may be considered sequentially, beginning with the LSB of X. In block 42', the process may determine if there are any remaining bits of X to consider. If there are, then the process may proceed to block 43' and may load a next coefficient, K_j , corresponding to the bit position of the LSB of X. The process may then proceed to block 44' and may compute the product, $Y \cdot K_j$. Then, in block 45', the process may, based on the value of the current LSB of X, determine whether to load the

product, $Y \cdot K_j$, as the next value of Y or to have Y remain the same. The process may then proceed to block 46' and may right-shift X, to provide a new LSB. The process may then loop back to block 42' to test if there are still bits to consider. If all bits of X have been considered, the process may proceed to block 47' in the case in which the apparatus operates only on the fractional portion of X. In block 47', the result obtained for the fractional portion of Y (corresponding to the fractional portion of X) may be left-shifted according to the integer portion of X, as discussed above, to account for the integer portion of X. After this shifting the process may be complete.

[0041] In some embodiments of the invention, the apparatus, e.g., as shown in Figures 3A-3E, may be integrated into or coupled to a computing platform, where the computing platform may include at least one microprocessor. An example of such a system according to some embodiments of the invention is shown in Figure 5. Figure 5 shows a processor 51 that may be coupled to the computational apparatus 53, for example, as embodied in one of Figures 3A-3E. The coupling may be by means of any suitable connection, which may comprise, but is not limited to, one or more buses, wireless pathways, optical pathways, shared memories, etc. The computing platform may use, for example, the above-described methods to use embodiments of the inventive apparatus 53 to compute logarithmic and/or exponential functions. In such a system, processor 51 may transmit, for example, operands and/or a function selection signal to computational apparatus 53. Similarly, computational apparatus 53 may transmit, for example, a result back to processor 51.

[0042] Processor 51 may be furnished with associated memory 52, and computational apparatus 53 may be furnished with associated memory 54. Memories 52 and 54 may

comprise any known or as yet to be discovered memory (e.g., RAM, ROM, etc.).

Memory 52 may, for example, be used by processor 51 to store data and/or software.

Memory 54 may, for example, be used by computational apparatus 53 to store coefficients and/or results. Additionally, memories 52 and 54 may be implemented in a common memory device, and in such a case, processor 51 and computational apparatus 53 may pass quantities between each other by storing them in shared memory locations. It may be noted, however, that all of the above are merely examples of implementations, and that the invention is not to be thusly limited.

[0043] Some embodiments of the invention, as discussed above, may be embodied in the form of software instructions on a machine-accessible medium. Such an embodiment is illustrated in Figure 6. The computer system of Figure 6 may include at least one processor 62, with associated system memory 61, which may store, for example, operating system software and the like. The system may further include additional memory 63, which may, for example, include software instructions to perform various applications. System memory 61 and additional memory 63 may be implemented as separate memory devices, they may be integrated into a single memory device, or they may be implemented as some combination of separate and integrated memory devices. The system may also include one or more input/output (I/O) devices 64, for example (but not limited to), keyboard, mouse, trackball, printer, display, network connection, etc. The present invention may be embodied as software instructions that may be stored in system memory 61 or in additional memory 63. Such software instructions may also be stored in removable media (for example (but not limited to), compact disks, floppy disks, etc.), which may be read through an I/O device 64 (for example, but not limited to, a floppy

disk drive). Furthermore, the software instructions may also be transmitted to the computer system via an I/O device 64, for example, a network connection; in this case, the signal containing the software instructions may be considered to be a machine-accessible medium.

[0044] The invention has been described in detail with respect to various embodiments, and it will now be apparent from the foregoing to those skilled in the art that changes and modifications may be made without departing from the invention in its broader aspects.

The invention, therefore, as defined in the appended claims, is intended to cover all such changes and modifications as fall within the true spirit of the invention.